

## **High School Math Pathways Symposium**

# Algebra 2 Course Updates









# 5. Algebra 2 Course Updates

## Facilitated by

- Margie Coleman, Kings Local Schools
- Steve Hiner, Columbus City Schools
- Scott Reveal, Cincinnati Public Schools
- Lee Wayand, Columbus State Community College

This session will be recorded, so it can be posted on the Department's website. The recording will begin at the end of this slide.



Give feedback on our Padlet!



# Algebra 2 Refocused

Goal: To get more students to understand and pass Calculus at the collegiate level.

College-level Calculus is just the *beginning* of mathematics for most STEM students on the Calculus Pathway.



## It is no longer Algebra 2 for all!





## Rigor "Students use mathematical language to communicate effectively and to describe their work with clarity and precision. Students demonstrate how, when, and why their procedure works and why it is appropriate. Students can answer the question, 'How do we know?'"







Rigorous courses are	Rigorous courses
Defined by complexity, which is a measure of the thinking, action or knowledge that is needed to complete the task	Characterized by on a measure of effort complete a task
Measured in depth of understanding	Measured by the a
Opportunities for precision in reasoning, language, definitions and notation that are sufficient to appropriate age/course	Based on procedu
Determined by students' process	Measured by assign problems
Opportunities for students to make decisions in problem solving	Defined only by th



are not...

## difficulty, which is rt required to

## amount of work

## ire alone

## gning difficult

### e resources used

Rigorous courses are	Rigorous courses
Opportunities to make connections	Taught in isolation
Supportive of the transfer of knowledge to new situations	Repetitive
Driven by students developing efficient explanations of solutions and why they work, providing opportunities for thinking and reasoning about contextual problems and situations	Focused on getting
Defined by what the student does with what you give them	Defined by what yo student



## s are not...

### g an answer

## ou give the



# **Higher Education Expectations**

- Algebraic Reasoning
- Analytic Reasoning
- Communication
- Independence



Ohio

of Education



**Communication and Analysis** 

Modeling with Functions

Extending Algebraic Reasoning

Polynomial and Rational Relationships

**Trigonometry of General Triangles** 









## Number and Quantity

## STANDARDS ADDED

#### Perform arithmetic operations with complex numbers.

**N.CN.3** Find the conjugate of a complex number; use conjugates to find magnitudes and quotients of complex numbers.

### **PLUS (+) SIGNS REMOVED**

#### Use complex numbers in polynomial identities and equations.

**N.CN.7** Solve quadratic equations with real coefficients that have complex solutions. **N.CN.8** Extend polynomial identities to the complex numbers. For example, rewrite  $x^2 + 4$  as (x + 2i)(x - 2i).

**N.CN.9** Know the Fundamental Theorem of Algebra; show that it is true for quadratic polynomials.







## Algebra

### STANDARDS DELETED

Use polynomial identities to solve problems.

**A.APR.4** Prove polynomial identities and use them to describe numerical relationships. *For example, the* polynomial identity  $(x^2 + y^2)^2 = (x^2 - y^2)^2 + (2xy)^2$  can be used to generate Pythagorean triples.

### **PLUS (+) SIGNS REMOVED**

#### **Rewrite rational expressions.**

**A.APR.7** Understand that rational expressions form a system analogous to the rational numbers, closed under addition, subtraction, multiplication, and division by a nonzero rational expression; add, subtract, multiply, and divide rational expressions.





10

## **Functions**

### STANDARDS ADDED

#### Build a function that models a relationship between two quantities.

**F.BF.1** Write a function that describes a relationship between two quantities.

**c.** Compose functions. For example, if T(y) is the temperature in the atmosphere as a function of height, and h(t) is the height of a weather balloon as a function of time, then T(h(t)) is the temperature of a cooling body by adding a constant function to a decaying exponential, and relate these functions to the model. (A2, M3).

### STANDARDS DELETED

All F.TF Standards





Department of Education

11

## **Functions**

#### PLUS (+) SIGNS REMOVED

Analyze functions using different representations.

**F.IF.7** Graph functions expressed symbolically and indicate key features of the graph, by hand in simple cases and using technology for more complicated cases. Include applications and how key features relate to characteristics of a situation, making selection of a particular type of function model appropriate.  $\star$ 

g. Graph rational functions, identifying zeros and asymptotes when factoring is reasonable, and indicating end behavior. (A2, M3)

**h.** Graph logarithmic functions, indicating intercepts and end behavior. (A2, M3)

**Build new functions from existing functions.** 

**F.BF.4** Find inverse functions.

**b.** Read values of an inverse function from a graph or a table, given that the function has an inverse. (A2, M3)

- c. Verify by composition that one function is the inverse of another. (A2, M3)
- **d.** Find the inverse of a function algebraically, given that the function has an inverse. (A2, M3)





## Geometry

### STANDARDS DELETED

Find arc lengths and areas of sectors of circles.

**G.C.6** Derive formulas that relate degrees and radians, and convert between the two. (A2, M3)





Department of Education

13

## Geometry

#### **PLUS (+) SIGNS REMOVED**

Define trigonometric ratios, and solve problems involving right triangles.

**G.SRT.8** Solve problems involving right triangles.

**b.** Use trigonometric ratios and the Pythagorean Theorem to solve right triangles in applied problems.  $\star$  (A2, M3)

Note: Standard G.SRT.10 Part a. is included in this course to be considered for next standards revision. Apply trigonometry to general triangles.

**G.SRT.9** Derive the formula  $A = \frac{1}{2} ab \sin(C)$  for the area of a triangle by drawing an auxiliary line from a vertex perpendicular to the opposite side.

**G.SRT.10** Explain proofs of the Laws of Sines and Cosines and use the Laws to solve problems. **a.** Extend right triangle trigonometry to include obtuse angles.

**G.SRT.11** Understand and apply the Law of Sines and the Law of Cosines to find unknown measurements in right and non-right triangles, e.g., surveying problems, resultant forces.





## Statistics and Probability

### STANDARDS DELETED

**All** Statistics and Probability standards except:

#### Summarize, represent, and interpret data on two categorical and quantitative variables.

**S.ID.6** Represent data on two quantitative variables on a scatter plot and describe how the variables are related  $\star$ 

- a. Fit a function to the data; use functions fitted to data to solve problems in the context of the data. Use given functions, or choose a function suggested by the context. Emphasize linear, quadratic, and exponential models. (A2, M3)
- Informally assess the fit of a function by discussing residuals. (A2, M3) b.





Department of Education

15

# **Follow-on Courses**

- Pre-Calculus at the high school
- CCP Trigonometry
- Other Algebra 2 equivalency course
- Other CCP math course
- Possibly AP Statistics

Note: CCP College Algebra is not a beneficial course for most students on the calculus pathway. It would be better for most students on the calculus pathway to take a pre-calculus course at their own high school with the intention of taking an AP Calculus course or Calculus in a postsecondary setting.





# Share your learning community with us! #MyOhioClassroom Celebrate educators! **#OhioLovesTeachers**

